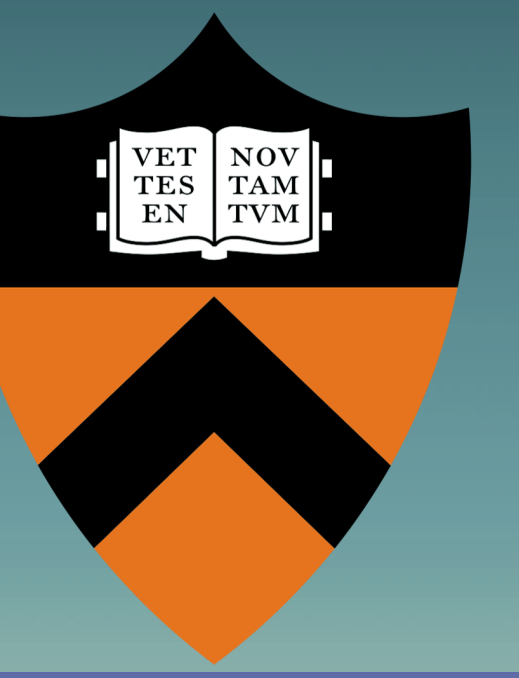


AUGMENTING LARGE REASONING MODELS WITH CONTRASTIVE GOAL-CONDITIONED RL



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MOTIVATION

As the paradigm in artificial intelligence shifts from pre-training scaling laws toward test-time training with RL, reasoning models have emerged as the next frontier. Ever since the release of DeepSeek-R1, a growing trend involves training on complex reasoning tasks with verifiable outcomes (i.e. reward of 1 if the solution is correct and 0 otherwise, with simple format rewards. We make the observation that this outcome-oriented reward paradigm is effectively a goal-conditioned setup.

Meanwhile, in the broader RL community, recent self-supervised RL algorithms have shown strong success on classical goal-conditioned settings, where sparse reward only provides a single bit of reward feedback for each trajectory. A core question thus arises: given this quasi-goal-conditioned paradigm in NLP, can these same goal-conditioned self-supervised RL methods be used to advance LLM reasoning?

INTRODUCTION

Contrastive RL: Contrastive RL [1] is a goal-conditioned method learns representations of state-action pairs ($\phi(s, a)$) and future states ($\psi(s_f)$) such that the representations of future states are closer than the representations of random states. Formally, we maximize the InfoNCE loss:

$$\mathcal{L}(s, a, s_f^+, s_f^-) \triangleq \log \sigma \left(\underbrace{f(s, a, s_f^+)}_{\phi(s, a)^T \psi(s_f^+)} \right) + \log(1 - \sigma \left(\underbrace{f(s, a, s_f^-)}_{\phi(s, a)^T \psi(s_f^-)} \right))$$

The final reward model captures the expected reward of achieving a goal state at intermediate reasoning steps.

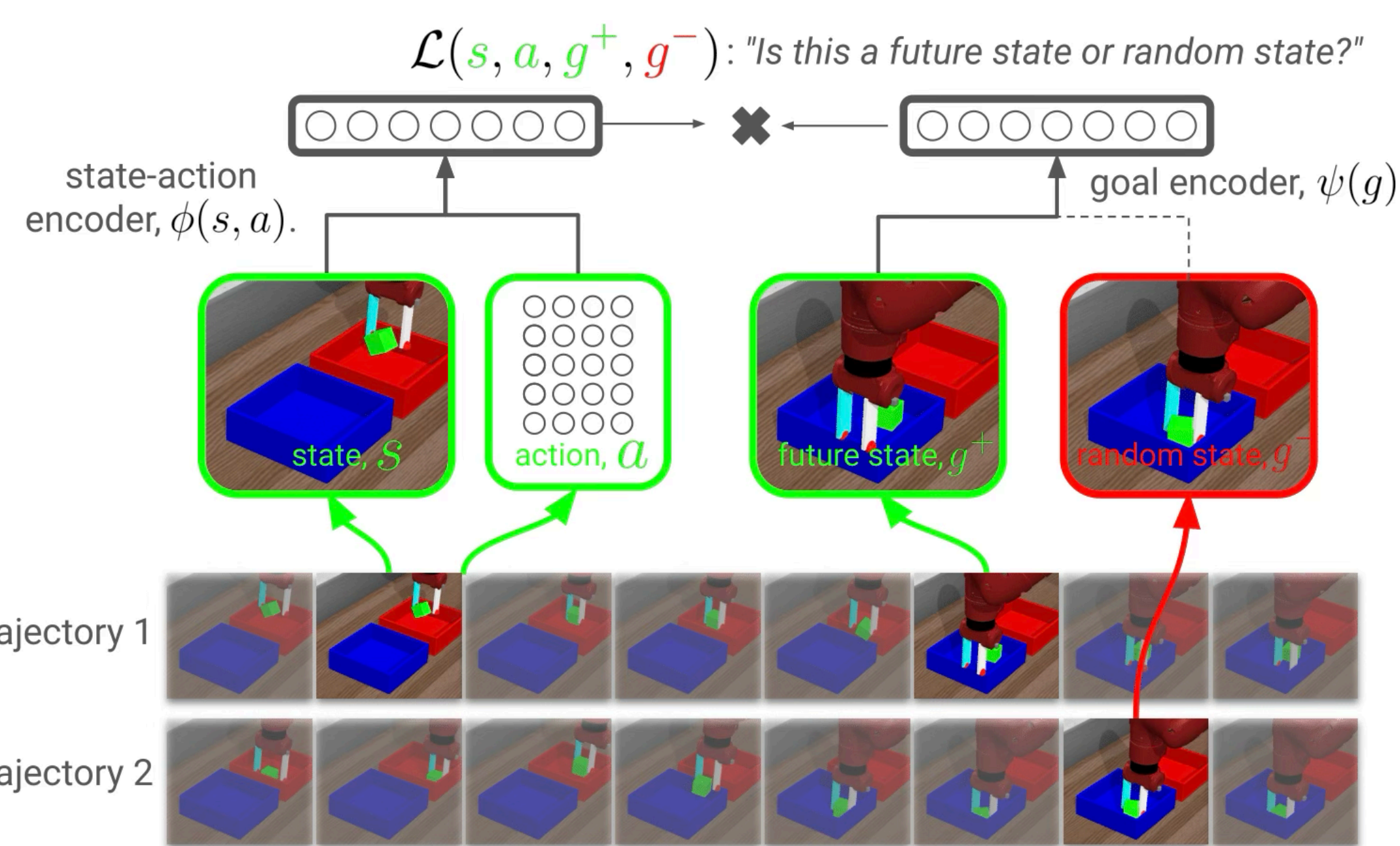


Figure 1: Classic example of GCRL for a robotics task [2].

Related Work: We build off LongProc’s [3] countdown benchmark prompt and validation pipeline to train our reward model. ScaleAI presented a method to train reward models using contrastive learning [4], but their method requires a human-labeled dataset of positive and negative examples, limiting generalizability. Our method requires no labels and works fully unsupervised.

APPROACH

State-Action-Goal Sampling

Trajectory 1

```
<Search Procedure>
Initial number set: [21, 16, 17, 26], target: 46

Pick two numbers (21, 16) (numbers left: [17, 26]). Try
possible operations. ### Current State: [21, 16, 17, 26]

|- Try 21 + 16 = 37. Add 37 to the number set. Current number
set: [37, 17, 26], target: 46. Options for choosing two numbers:
[(37, 17), (37, 26), (17, 26)]. ### Current State: [37, 17, 26]
...
|- Try 37 + 17 = 54. Add 54 to the number set. Current number
set: [54, 26], target: 46, just two numbers left. ###

Current State: [54, 26]

|- Try 54 + 26 = 80. Evaluate 80 != 46, drop this branch. ###
Current State: [80]
...
Current State: [20, 26]

|- Try 26 + 20 = 46. Evaluate 46 == 46, target! ### Current
State: [46]
</Search Procedure>
```

State

Action

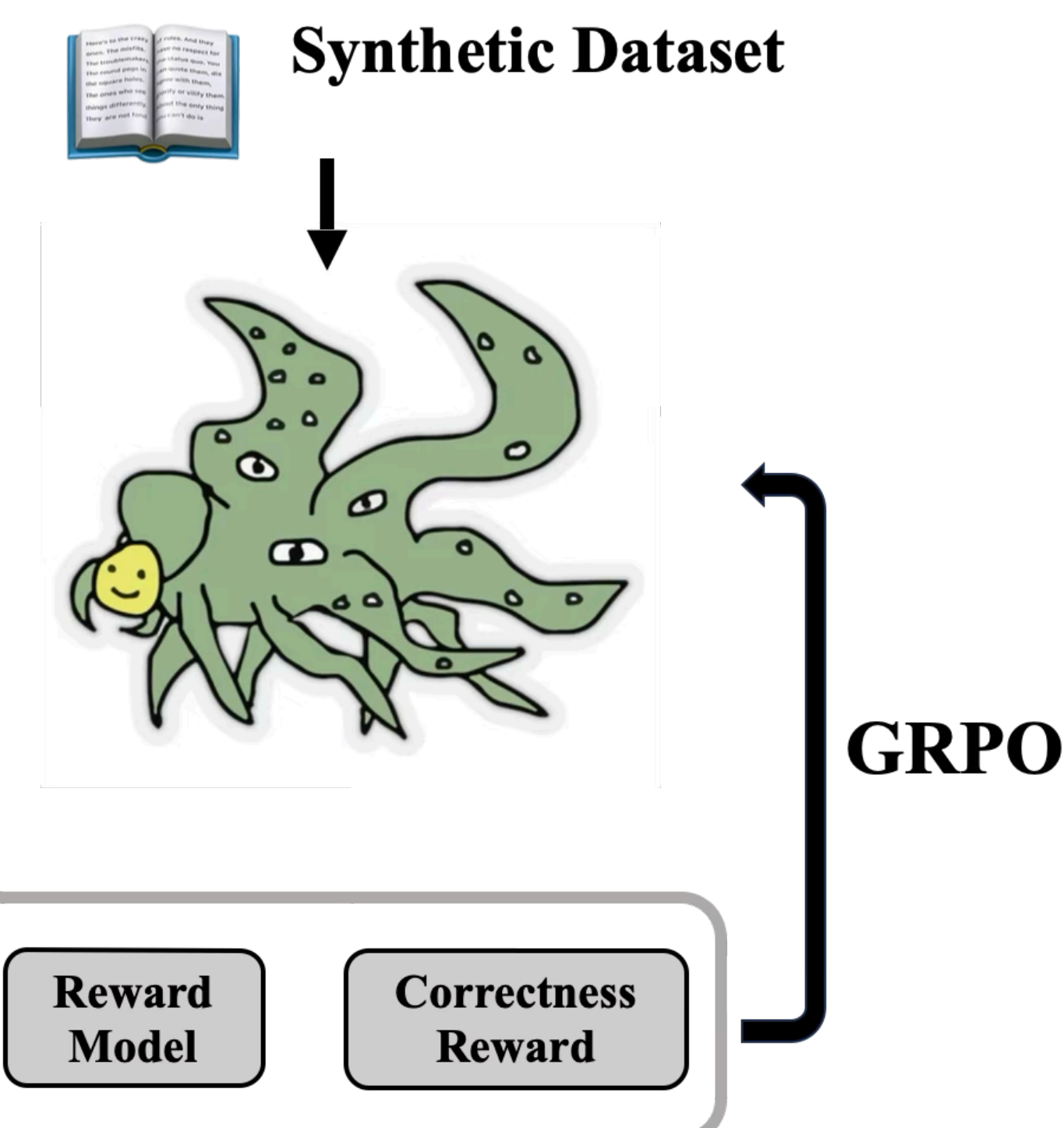
Future Goal

Random Goal

Trajectory 2

```
...
Current State: [336, 442]
...
```

GRPO Finetuning



Critic Model Rewards

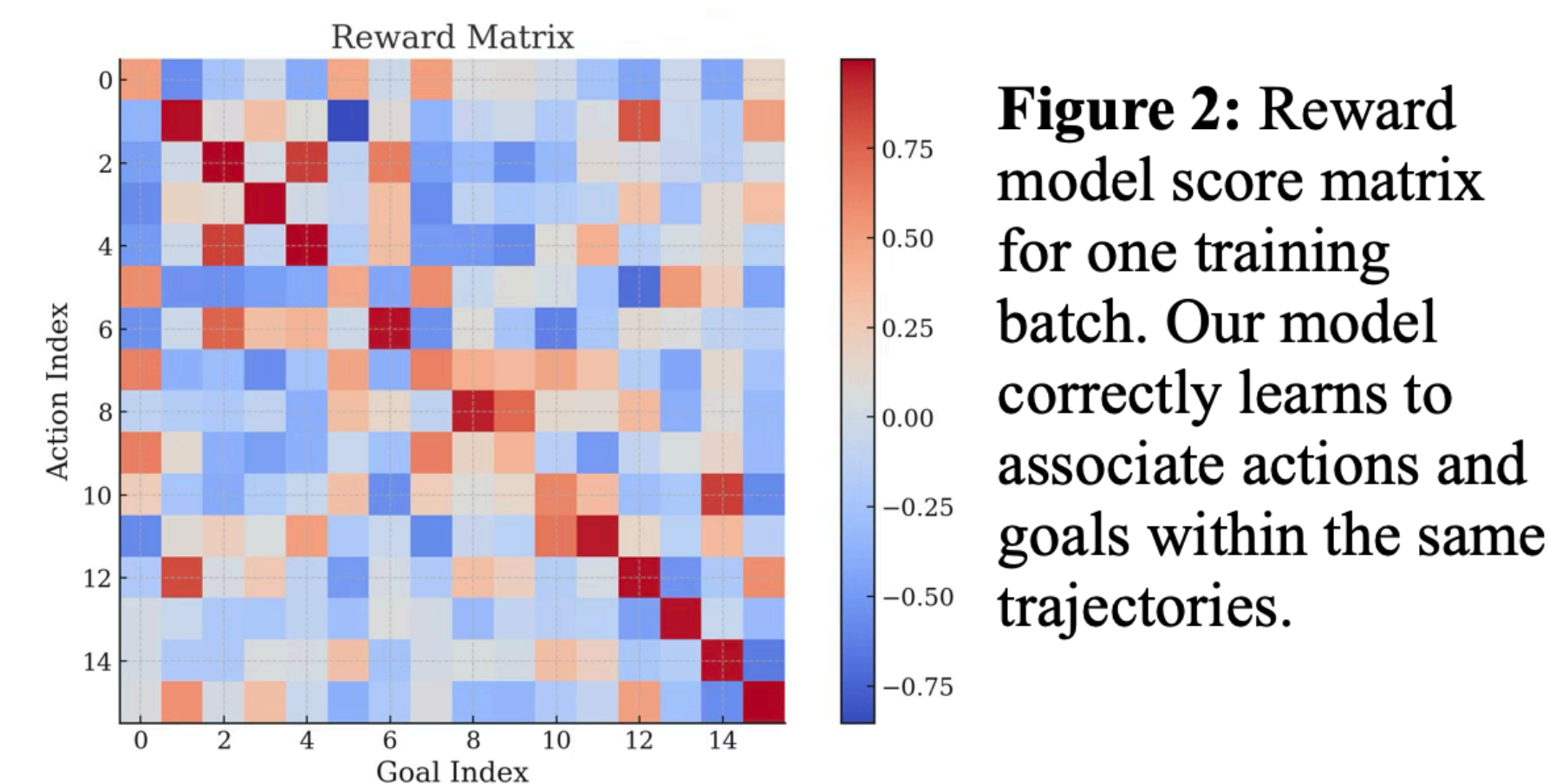


Figure 2: Reward model score matrix for one training batch. Our model correctly learns to associate actions and goals within the same trajectories.

Figure 2. Reasoning traces are split into state-action pairs, each matched with a later goal from the same trace. A pretrained LM is fine-tuned on the resulting triples via GRPO, while a contrastive critic (heat-map) learns dense rewards that align actions with future goals. The improved policy then generates new traces, which are resampled into fresh triples, closing a self-supervised actor-critic loop for goal-conditioned reasoning.

Critic Model Architectures

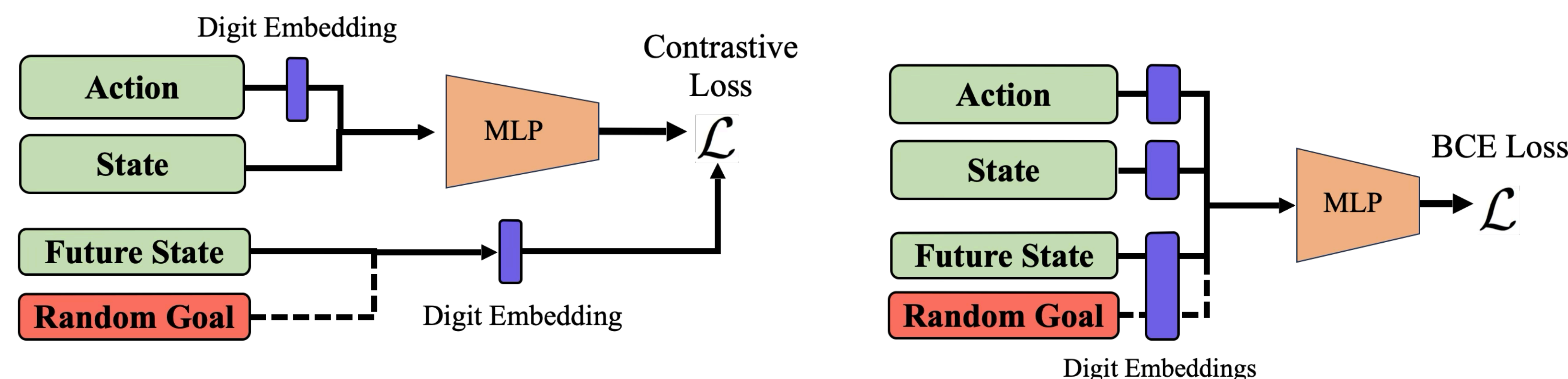


Figure 3: Architectures experimented on for the critic model. We found that the left architecture using a contrastive loss was insufficiently expressive because it relies on dot-product similarity to compare the state-action and goal embeddings.

CONTRASTIVE CRITIC

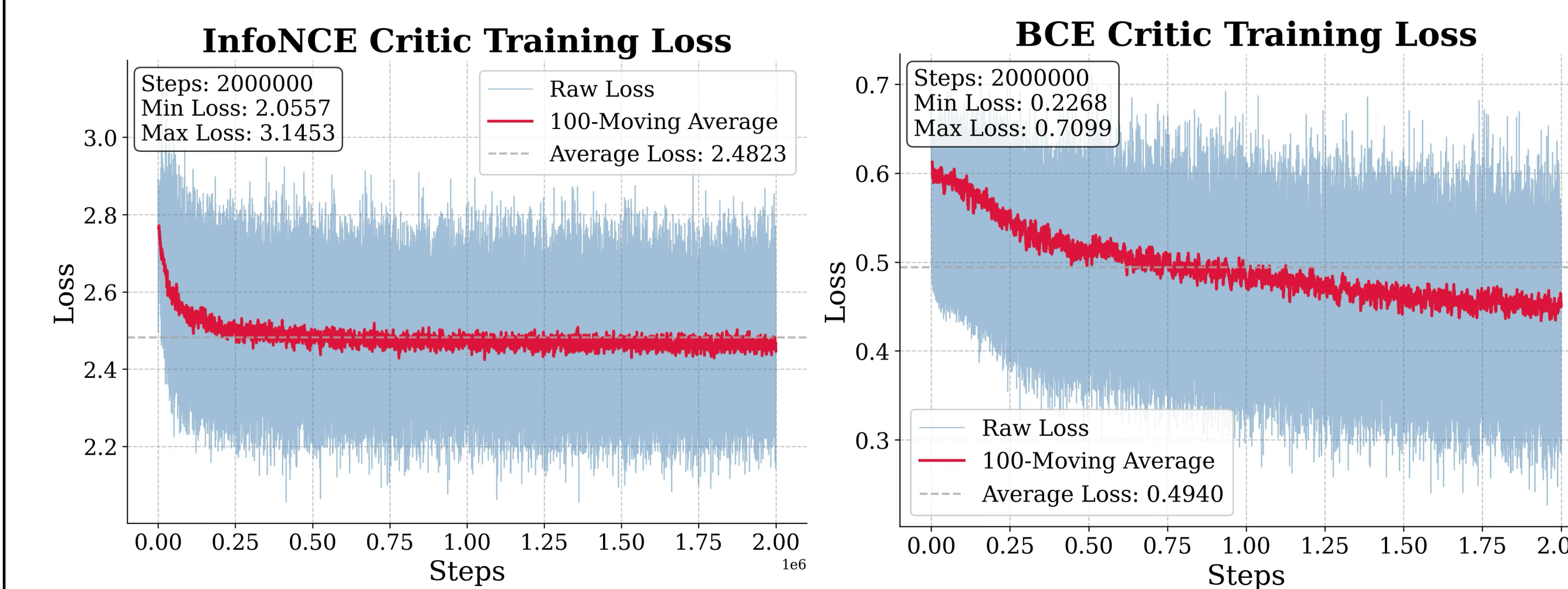


Figure 4: We train our critic models on 2,000,000 synthetic examples extracted from 100,000 procedurally generated trajectories to associate goals with trajectories.

GRPO RESULTS

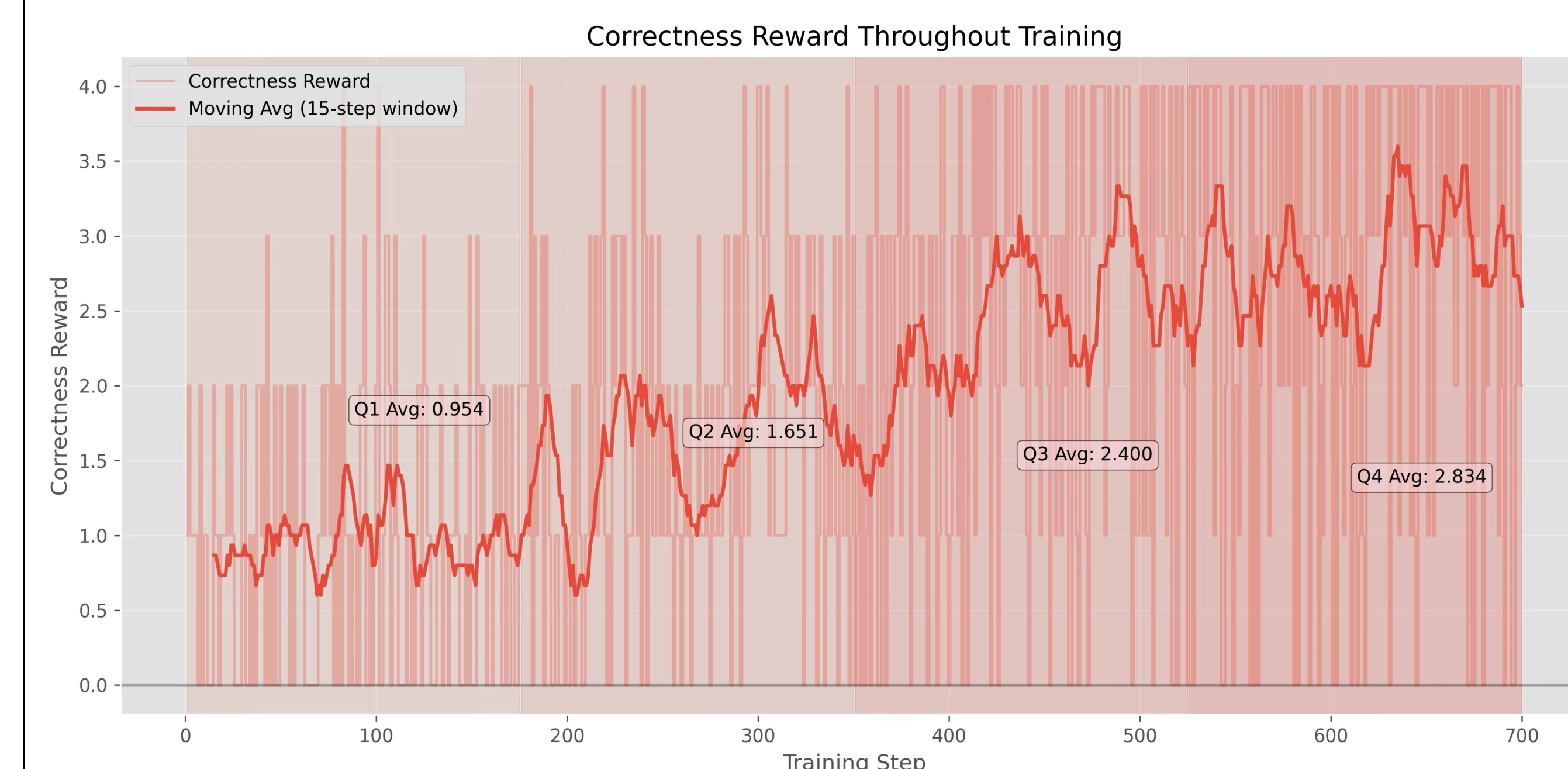


Figure 5: Baseline success rate over time during GRPO without contrastive loss.

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