Augmenting Large Reasoning Models with Contrastive Goal-Conditioned Reinforcement Learning

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1 Abstract

As the paradigm in artificial intelligence shifts from pre-training scaling laws toward test-time training with RL, reasoning models have emerged as the next frontier. Ever since the release of DeepSeek-R1 (DeepSeek-AI et al., 2025), a growing trend involves training on complex reasoning tasks with verifiable outcomes (i.e. reward of 1 if the solution is correct and 0 otherwise, with simple format rewards). We make the observation that this outcome-oriented reward paradigm is effectively a goal-conditioned setup. Meanwhile, in the broader RL community, recent self-supervised RL algorithms have shown strong success on classical goal-conditioned settings (Eysenbach et al., 2023), where sparse reward only provides a single bit of reward feedback for each trajectory. A core question thus arises: given this quasi-goal-conditioned paradigm in NLP, can these same goal-conditioned self-supervised RL methods be used to advance LLM reasoning?

2 Introduction

Large Language Models (LLMs) trained to reason using reinforcement learning (RL) have led a paradigm shift from pre-training compute scaling to inference time compute scaling (DeepSeek-AI et al., 2025; Muennighoff et al., 2025). The *reward models* (RMs) that evaluate output quality and guide training are therefore a critical piece of modern reasoning model training.

Existing frontier reasoning models are predominantly trained with outcome-based reward models (ORMs) that consist of a numerical verifier for complex math and coding tasks (DeepSeek-AI et al., 2025). The simplicity of the RM enables training on large corpora of verifiable problems without requiring any human feedback or labeling. However, ORMs provide a sparse reward structure and only provide feedback at the end of completions. Meanwhile, process reward models (PRMs) (Lightman et al., 2023) solve this problem by giving feedback at intermediate reasoning steps, thereby providing a dense reward structure. However, PRMs either require human-annotated trajectories, which are not scalable, or language-model based annotations that are noisy.

Drawing from the success of contrastive representation learning in traditional RL tasks (Eysenbach et al., 2023), we propose a novel technique for the self-supervised learning of a contrastive reward model, allowing the benefits of dense feedback signals while only requiring problems paired with a numerical verifier for the training of both the reward model and the reasoning model.

We test our approach on two leading openweight large language models, Qwen 2.5-7B (Yang et al., 2024) and Llama 3.1-8B (Grattafiori et al., 2024) on the game of countdown and investigate the challenges of contrastive representation learning for reward models. Code is available at github.com/dshah02/ContrastiveReasoners.

3 Related Work

Reinforcement Learning for LLMs.

To ensure language models accurately follow the preferences of users and can answer user queries beyond responding with the most likely next token, language models often undergo reinforcement learning-based post-training after self-supervised training on a language corpus to align better with human preference.

Language models can be treated as actors in a Markov Decision Process, with the prior input constituting their state and the choice of next token being the relevant actions. To incentivize behavior aligned with human desires, these language models can then receive a reward corresponding to the quality of their outputs, and using traditional methods from reinforcement learning, this reward can be used to update the weights of the language model to ensure better alignment with human feedback.

As human-provided grading is unscalable, the most common approach for aligning language models is known as Reinforcement Learning from Human Feedback (Ouyang et al., 2022), whereby human-annotated data on the quality of text, as aligned with human preferences, is collected on a wide variety of input text, and a separate reward language model is trained to predict, for any piece of text, the expected score it would receive from a human annotator. By prompting the base language model on a variety of queries, this reward model can be used to provide feedback on the policy, and when combined with Proximal Policy Optimization (PPO) (Schulman et al., 2017), will lead to a language model that retains the language knowledge of the base pre-trained model while being more likely to earn favorable scores from human reviewers.

However, for questions with concrete verifiable answers, such as mathematics and factual problems, the reward signal does not need to be provided from a reward model, but can instead be based on whether the model correctly answered the question. Shao et al. (2024); DeepSeek-AI et al. (2025) showed that training a language model based on this verifiable reward, leveraging Group Relative Policy Optimization (GRPO) (Shao et al., 2024), can lead to models with impressive performance on complex tasks and lead to the emergence of reasoning behavior. However, note that as only a single reward is provided per model completion, the aforementioned reward techniques are extremely sparse and thus perhaps computationally inefficient.

To provide greater signal, other practitioners employ process reward models, which aim to provide a reward on each token generated rather than on the entire completion (Nath et al., 2024). Although this reward is more dense, it is also much more challenging to train, as it can be difficult to evaluate each new token without the knowledge of what future tokens may be. PRMs currently require labeled output trajectories to train a reward model on distinguishing which token-level outputs are more likely to lead to a goal with the desired label (such as "Correct"); however, training these PRMs proves challenging as human-annotated reasoning trajectories are costly to obtain and LLM-annotated data is often faulty.

Contrastive Reward Models

Hejna et al. (2024); Nath et al. (2024) propose a procedural reward model that, although requiring human-labeled trajectories, provides a different approach to training procedural reward models based on learning trajectory embeddings. Rather than predicting a reward for each subset of text, Nath et al. (2024) propose learning a feature embedding ϕ from text to \mathbb{R}^n that preserves that text generated from the same trajectory are likely to map near each other. In this manner, a reward signal can be provided at the token-level by determining whether, at each step, the chosen action leads to an embedding closer to the goal embedding, with the goal embedding chosen as an average of the embeddings of successful trajectory embeddings during training.

Following (Nath et al., 2024), at a more technical level, with a dataset \mathcal{D} of inputs x paired with correct trajectories y_w and incorrect trajectories y^{ℓ} , we will learn a reward function r(x, y) = $r'(\phi(y_T|y_{\{0,...,T-1\}}, x))$, consisting of ϕ : text \rightarrow \mathbb{R}^n and $r' : \mathbb{R}^n \rightarrow \mathbb{R}^1$. To learn the feature embedding ϕ and reward mapping r', we then aim to minimize a combined loss $\mathcal{L}^R + \lambda \mathcal{L}^C$, where

$$\mathcal{L}^{R} = -\frac{1}{|\mathcal{D}|} \mathbb{E}_{(x, y^{w}, y^{\ell}) \sim \mathcal{D}} \log(\sigma(r(x, y^{w}) - r(x, y^{\ell}))$$

incentivizes rewarding correct trajectories and

$$\mathcal{L}^{C} = \mathbb{E}_{(x,y_{0,t},y_{g}^{+},y_{g}^{-})} \log \left(\frac{\sigma(f(x,y_{\{0,\dots,t\}},y_{g}^{+}))}{1 - \sigma(f(x,y_{\{0,\dots,t\}},y_{g}^{-}))} \right)$$

incentivizes the model to correctly embed trajectories in-progress near their end-state and away from the end-state of other trajectories. The function $f(x, y_{0,...t}, y_g)$ is the cosine similarity between $\phi(x, y_g)$ and $\phi(x, y_{0,...,t})$, and $y_{0,...t}$ is a randomly chosen prefix of y_g^+ , while y_g^- is from a different trajectory with the same prompt (Nath et al., 2024).

Countdown Task and LongProc

To measure reasoning performance on a verifiable task, we choose the countdown problem (Ye et al., 2025; Yao et al., 2023). Each countdown problem consists of a list of 4 numbers and a target number to create based on those 4 numbers and the 4 basic arithmetic operations $+, -, \times, \div$. For instance, an example might be [3, 5, 2, 6] with a goal of creating 8, and a correct answer is $(6-2) \times (5-3)$. Another correct answer is $(6 \times 3) - (5 \times 2)$. We leverage the LongProc (Ye et al., 2025) countdown benchmark in order to construct example problems and train our model. We consider the easiest set of LongProc Countdown problems, which predominantly consists of tasks requiring addition and subtraction and can be solved by procedural generation software in less than 500 tokens. Each prompt showcases an example of correctly answering a countdown problem and a description of how the model should attempt the problem.

The countdown problem has been used as a classic example of a reasoning task (Yao et al., 2023) and harder examples can be quite challenging for many people.¹

As a reference for baseline model performance, under the LongProc Countdown prompting method, which has models attempt the problem via breadthfirst search with 500 tokens, Llama 3.1-8B (Instruct) answers the easiest set of problems with 8% accuracy and Qwen 2.5-7B (Instruct) achieves 32% accuracy. For our testing, we permit the models 1024 tokens and modify the prompt, so although our results are not directly comparable, this serves as a baseline to gauge problem difficulty.

4 Approach

4.1 Contrastive Critic Design

Our primary goal is to train a critic model to understand whether an intermediate state in a reasoning trajectory is "on the right track" towards achieving the final goal. We want the critic to learn to map (intermediate state, current action) pairs and final goals into a shared embedding space. In this learned space, the embedding of a state-action pair that is part of a successful trajectory leading to a specific goal should be "close" to the embedding of that goal. Conversely, it should be "far" from embeddings of irrelevant goals or goals corresponding to different problems. To achieve this, we employ a contrastive training setup, specifically the InfoNCE (van den Oord et al., 2019) loss. This approach allows for dense feedback without requiring explicit step-by-step human labels, relying instead on the final outcome and the trajectory structure. Our design is also motivated by the work of (Nath et al., 2024), although we strive to make our method purely self-supervised.

4.2 Text-based Critics

We experimented with several different critic model architectures, as illustrated in Figure 1. Initially, we attempted to train a model that would extract embeddings from the text output of a given trajectory. In this setup, we fine-tuned a small language model, such as Rho-Math-1B (Lin et al., 2025), to use as the critic model. We randomly sampled some action \mathcal{A} as a randomly chosen line within the reasoning trace, and then considered the state Sto be the entire reasoning prefix that preceded that line. The goals \mathcal{G} were randomly sampled lines that came after the action. We extracted the goal and state-action embeddings from the activations of the language model and trained it using a standard contrastive loss. The primary issue with this method was that it had an extremely poor speed/accuracy tradeoff. Even relatively small 3B models were prohibitively slow at both train and inference time, and smaller models struggled to learn any useful signal at all.

4.3 Numerical Critics

As such, we switched to a lightweight, task-specific architecture. We observed that the core task of the critic model was merely to determine whether some intermediate set of numbers \mathcal{X} was "on-theright-track" to reach some goal set of numbers \mathcal{Y} . Instead of recovering embeddings from text containing numerical values, we decided to directly extract numerical values to use as inputs to our critic model.

Our first revised architecture (Figure 1B) consisted of digit embeddings layers that took in the initial array of four numbers as the state S, a randomly sampled intermediate array as the action A, and a randomly sampled array that comes after the action as the goal G. The state-action pair is passed through a digit embedding and concatenated. The concatenated vector is then passed through a multilayer projection head to obtain the state-action embedding. Meanwhile, the sampled goal is passed through a separate digit embedding to obtain the goal embedding. With these two embeddings, we train the network using the same contrastive loss.

This network was significantly faster to run due to being under 1M total parameters and achieved significantly better training accuracy. However, we found that adding the critic model had relatively little impact on RL training. By probing the critic network with sample state-action goal pairs, we

¹If you want to challenge yourself, try to make 20 from [8, 3, 7, 6] or to find both ways to make 8 from [3, 4, 5, 7].

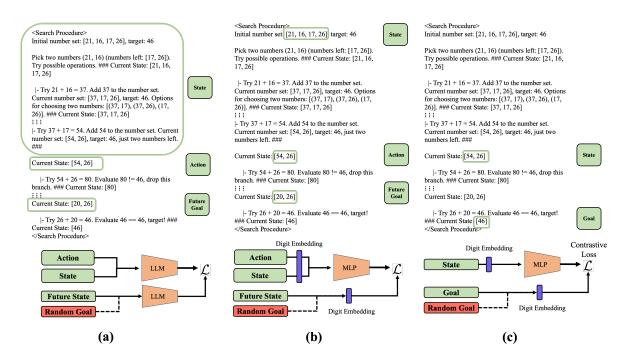


Figure 1: Overview of the three critic model architectures explored. (A) Text-based Critic: Uses a language model to extract embeddings from textual representations of state, action, and goal. (B) Numerical Critic V1: Employs digit embeddings for an initial array (state), an intermediate array (action), and a future array (goal). (C) Numerical Critic V2 (Final Architecture): Uses digit embeddings for an intermediate array (state) with the fixed final target value serving as the goal. The sampling strategy for state-action-goal triplets is shown above each respective architecture design.

found the network was not learning robust associations between the action and the goal. Instead, because the model had access to the initial set, it was circumventing the difficult task of predicting whether the intermediate action could lead to the goal and instead only learning whether the future sampled goal could be achieved with the initial four numbers. However, this representation is almost useless at inference time because the goal is *always achievable* given the initial numbers by construction. In fact, when we visualized the critic model's goal embedding space, we found that it learned a trivial even-odd partitioning of values (Figure 2).

To address this problem, we remove the initial array as input and then fix the goal \mathcal{G} as the final target value, instead of randomly sampling a future state (Figure 1C). This lets the model directly learn representations from intermediate states for a single target value, which is what we desire at inference time. Intuitively, the model must learn whether target value Z can be made from some intermediate state [A, B, C] (or [A, B]). Visualizing the goal embeddings space of this architecture reveals that the model learns a far more informative distribution of goals (Figure 3).

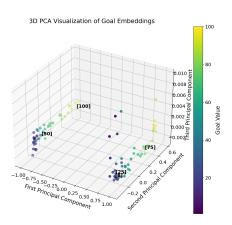


Figure 2: PCA visualization of the goal embedding space for the first numerical critic. The critic learned a trivial partitioning of values based on parity, indicating it was not capturing the desired relationships for progressing towards the target value.

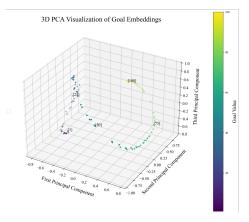


Figure 3: PCA visualization of the goal embedding space for our second numerical critic. This architecture, which uses the fixed final target value as the goal and only intermediate states as input, learns a more informative and structured distribution of goal embeddings.

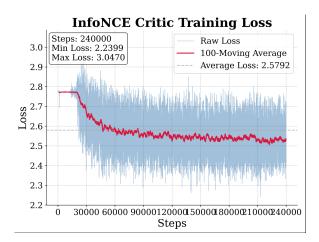


Figure 4: Training loss curve for the final critic model. The contrastive loss steadily decreases over 240,000 training steps, indicating successful convergence of the critic.

5 Experiments

5.1 Critic Model Training

We construct a large synthetic dataset of several hundred thousand unique trajectories using Long-Proc's procedural data generator, which creates step-by-step, natural language traces for the countdown game that correspond to a simple depth-firstsearch. We train our critic model on this synthetic dataset for 240000 steps with a batch size of 16 state action pairs from different trajectories. Our critic model successfully converges as seen in Figure 4. We visualize the effectiveness of the contrastive training by examining the cosine similarity matrix of state-action versus goal embeddings for a batch, as shown in Figure 5.

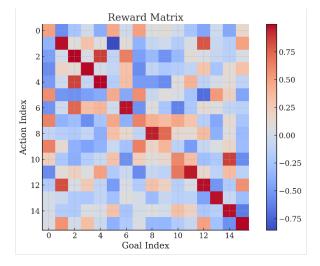


Figure 5: Heatmap of the similarity matrix between state-action embeddings and goal embeddings for a batch of 16 samples during critic model training. The strong diagonal indicates that positive pairs (state-action and goal embeddings from the same trajectory fragment) have higher similarity than negative pairs, demonstrating the effectiveness of the contrastive learning objective.

5.2 LLM Training

We run Group Relative Policy Optimization (GRPO) for the countdown task on Qwen2.5-7B and Llama-3.1-8B-Instruct to evaluate our reward model. We used the LongProc countdown dataset for training data and the LongProc countdown verifier for verification rewards. All models are trained for 1500 steps. We first trained the baseline models using only the verification outcome reward model. The Qwen model achieves approximately an 80% sucess rate. Meanwhile the Llama model struggles, rising to around 75% success rate through a less stable trajectory. This behavior is expected, because Ye et al. (2025) observed that the base Qwen model is much stronger at countdown than Llama. As such, Qwen easily achieves a extremely high success rate, while Llama suffers from higher variability when learning due to its lower initial capabilities and sparse reward feedback.

When training with our critic model feedback in addition to the standard verification reward, we find that Qwen's performance slightly to around 70% success rate while Llama decreases to about a 63% success rate. However, we note that our critic did slightly improve LLama's training in the first half of training. We hypothesize that the performance drop is because the critic is somewhat noisy, which might be a detriment once the model is at a suffi-

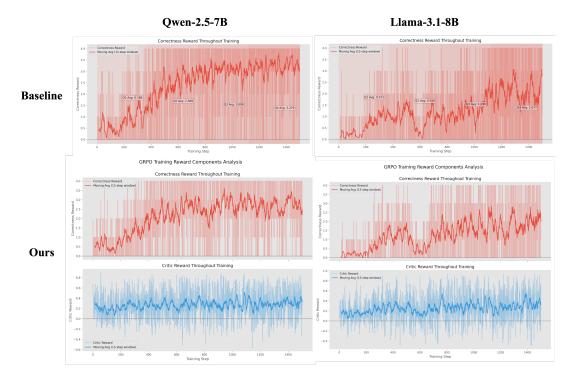


Figure 6: Group Relative Policy Optimization (GRPO) results on the countdown task for Qwen 2.5-7B (left) and Llama 3.1-8B (right). Performance is measured by success rate over 1500 training steps. The graphs compare the baseline model trained with only outcome-based rewards (GRPO Baseline) against the model augmented with our contrastive critic model (GRPO + Contrastive Critic).

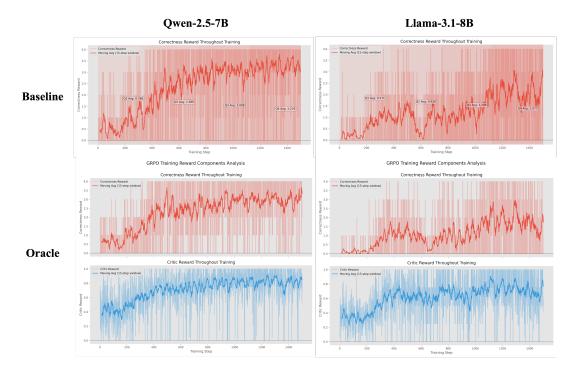


Figure 7: GRPO results on the countdown task for Qwen 2.5-7B (left) and Llama 3.1-8B (right). Performance is measured by success rate over 1500 training steps. The graphs compare the baseline model trained with only outcome-based rewards (GRPO Baseline) against the model augmented with Oracle critic feedback, where the Oracle critic uses brute-force searching to reward the model only if it makes the perfect move. We note that over the course of training, Oracle critic rewards increase, corresponding to the model's improveds searching performance.

ciently high level of performance. This would explain why the Llama model trained with our critic has slightly better performance early on, when the noisy critic model is helpful, but ultimately achieves a lower performance. These results, illustrated in Figure 6, suggest that our method might be more promising and show better results on even smaller base models that would otherwise be too weak to have convergent/stable RL training.

We additionally experiment with an oracle critic model that algorithmically computes whether the goal state is achievable, instead of learning it contrastively. We observe that the Qwen model trained with an additional oracle critic achieves better performance than the baseline (90% vs 80%), which further suggests that the noisy results of our trained critic model contributes to the decline in RL performance. The results of the experiments with the oracle model are illustrated in Figure 7.

5.3 Tools

All experimentation was done in PyTorch (Paszke et al., 2019) and our code-base is dervied from the Unsloth Llama 3.1 GRPO notebook (Unsloth.ai, 2025) and LongProc's countdown task code (Ye et al., 2025).

6 Conclusion

We have demonstrated a proof-of-concept contrastive reward model that can aid RL training of large language models on reasoning tasks. However, our method still faces several limitations. First, our critic model architecture is task-specific; ideally, the initial language model architecture should be used for the most task flexibility given sufficient compute. Second, we evaluate on a toy reasoning task for which we can generate large amounts of synthetic data for offline. A significant challenge remains developing a technique to train the critic model in conjunction with the base model on online trajectories, which will allow this method to be applied to a broader range of tasks.

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